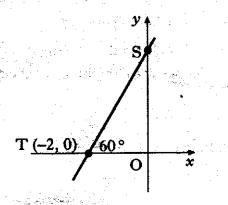
ALL questions should be attempted.

Marks

3

1. Find the equation of the line ST, where T is the point (-2, 0) and angle STO is 60°.



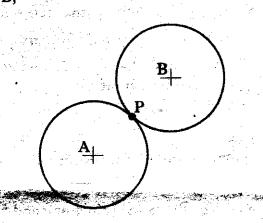
2. Two congruent circles, with centres A and B,

Relative to suitable axes, their equations are

$$x^{2} + y^{2} + 6x + 4y - 12 = 0$$
 and $x^{2} + y^{2} - 6x - 12y + 20 = 0$.

touch at P.

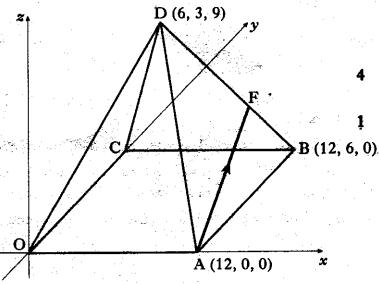
- (a) Find the coordinates of P.
- (b) Find the length of AB.



3. D,OABC is a pyramid. A is the point (12, 0, 0), B is (12, 6, 0) and D is (6, 3, 9).

F divides DB in the ratio 2:1.

- (a) Find the coordinates of the point F.
- (b) Express \overrightarrow{AF} in component form.



- 4. Functions f(x) = 3x 1 and $g(x) = x^2 + 7$ are defined on the set of real numbers.
 - (a) Find h(x) where h(x) = g(f(x)).

2

- (b) (i) Write down the coordinates of the minimum turning point of y = h(x).
 - (ii) Hence state the range of the function h.

2

5. Differentiate $(1 + 2 \sin x)^4$ with respect to x.

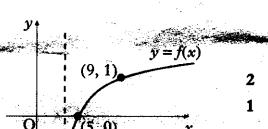
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- 6. (a) The terms of a sequence satisfy $u_{n+1} = ku_n + 5$. Find the value of k which produces a sequence with a limit of 4.
 - (b) A sequence satisfies the recurrence relation $u_{n+1} = mu_n + 5$, $u_0 = 3$.
 - (i) Express u_1 and u_2 in terms of m.
 - (ii) Given that $u_2 = 7$, find the value of m which produces a sequence with no limit.

5

7. The function f is of the form $f(x) = \log_b (x - a)$.

The graph of y = f(x) is shown in the first factor.



- (a) Write down the values of a and b.
- (b) State the domain of f.

- 8. A function f is defined by the formula $f(x) = 2x^3 7x^2 + 9$ where x is a real number.
 - (a) Show that (x-3) is a factor of f(x), and hence factorise f(x) fully.

5

- (b) Find the coordinates of the points where the curve with equation y = f(x) crosses the x- and y-axes.
- 2
- (c) Find the greatest and least values of f in the interval $-2 \le x \le 2$.

5

9. If $\cos 2x = \frac{7}{25}$ and $0 < x < \frac{\pi}{2}$, find the exact values of $\cos x$ and $\sin x$.

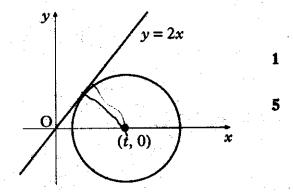
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5

- 10. (a) Express $\sin x \sqrt{3}\cos x$ in the form $k\sin(x-a)$ where k > 0 and $0 \le a \le 2\pi$.
 - (b) Hence, or otherwise, sketch the curve with equation $y = 3 + \sin x \sqrt{3} \cos x$ in the interval $0 \le x \le 2\pi$.
- 11. (a) A circle has centre (t, 0), t > 0, and radius 2 units.

Write down the equation of the circle.

(b) Find the exact value of t such that the line y = 2x is a tangent to the circle.



END OF QUESTION PAPER]