

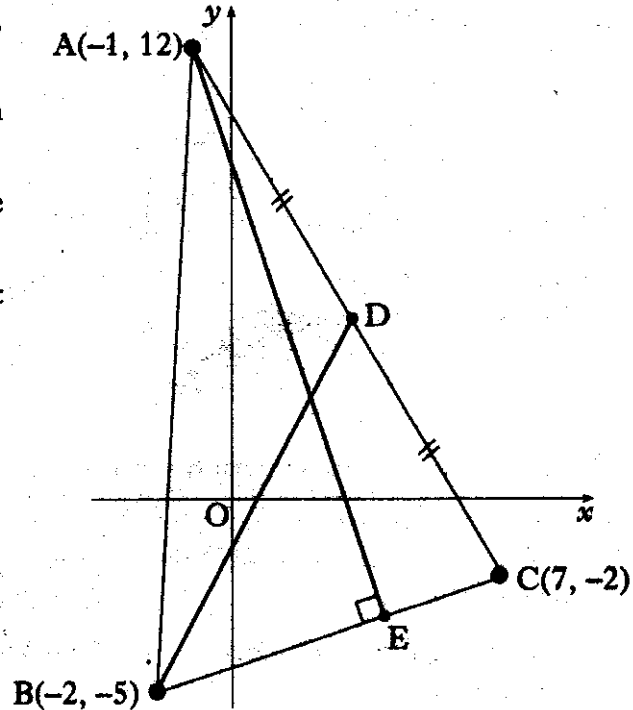
HIGHER 2006 PAPER 1

ALL questions should be attempted.

Marks

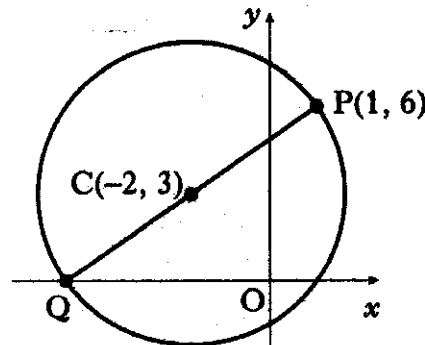
1. Triangle ABC has vertices $A(-1, 12)$, $B(-2, -5)$ and $C(7, -2)$.

- (a) Find the equation of the median BD. 3
 (b) Find the equation of the altitude AE. 3
 (c) Find the coordinates of the point of intersection of BD and AE. 3



2. A circle has centre $C(-2, 3)$ and passes through $P(1, 6)$.

- (a) Find the equation of the circle. 2
 (b) PQ is a diameter of the circle. Find the equation of the tangent to this circle at Q. 4



3. Two functions f and g are defined by $f(x) = 2x + 3$ and $g(x) = 2x - 3$, where x is a real number.

- (a) Find expressions for:

(i) $f(g(x))$;

(ii) $g(f(x))$. 3

- (b) Determine the least possible value of the product $f(g(x)) \times g(f(x))$. 2

[Turn over

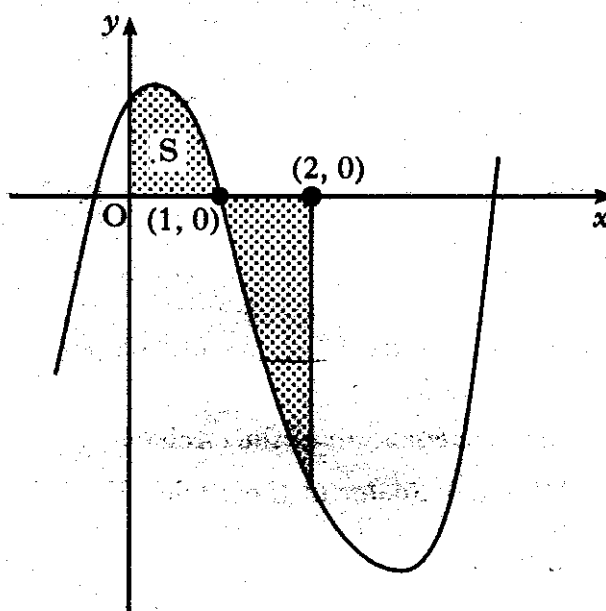
4. A sequence is defined by the recurrence relation $u_{n+1} = 0.8u_n + 12$, $u_0 = 4$.
- (a) State why this sequence has a limit. 1
- (b) Find this limit. 2

5. A function f is defined by $f(x) = (2x - 1)^5$.
- Find the coordinates of the stationary point on the graph with equation $y = f(x)$ and determine its nature. 7

6. The graph shown has equation $y = x^3 - 6x^2 + 4x + 1$.

The total shaded area is bounded by the curve, the x -axis, the y -axis and the line $x = 2$.

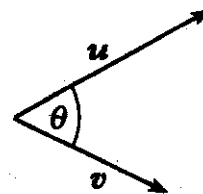
- (a) Calculate the shaded area labelled S.
- (b) Hence find the total shaded area.



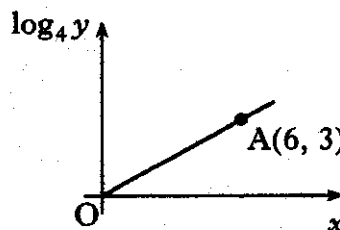
7. Solve the equation $\sin x^\circ - \sin 2x^\circ = 0$ in the interval $0 \leq x \leq 360$. 4

8. (a) Express $2x^2 + 4x - 3$ in the form $a(x + b)^2 + c$. 3
- (b) Write down the coordinates of the turning point on the parabola with equation $y = 2x^2 + 4x - 3$. 1

9. u and v are vectors given by $u = \begin{pmatrix} k^3 \\ 1 \\ k+2 \end{pmatrix}$ and $v = \begin{pmatrix} 1 \\ 3k^2 \\ -1 \end{pmatrix}$, where $k > 0$.



- (a) If $u \cdot v = 1$, show that $k^3 + 3k^2 - k - 3 = 0$. 2
- (b) Show that $(k + 3)$ is a factor of $k^3 + 3k^2 - k - 3$ and hence factorise $k^3 + 3k^2 - k - 3$ fully. 5
- (c) Deduce the only possible value of k . 1
- (d) The angle between u and v is θ . Find the exact value of $\cos \theta$. 3
10. Two variables, x and y , are connected by the law $y = a^x$. The graph of $\log_4 y$ against x is a straight line passing through the origin and the point A(6, 3). Find the value of a . 4



[END OF QUESTION PAPER]